

$$\theta < 0$$

واجب 27

$$\csc \theta = -\sqrt{5}$$

انطلاق
مقام

$$\begin{aligned} & \frac{-1}{\sqrt{5}} \cdot \frac{\sqrt{5}}{\sqrt{5}} \\ &= -\frac{\sqrt{5}}{5} \end{aligned}$$

$$\textcircled{1} \sin \theta = \frac{-1}{\sqrt{5}} = \frac{-\sqrt{5}}{5}$$

$$\textcircled{2} \cot \theta \Rightarrow 1 + \cot^2 \theta = \csc^2 \theta$$

$$\cot^2 \theta = (-\sqrt{5})^2 - 1$$

$$\cot^2 \theta = 4 \rightarrow \cot \theta = \pm 2$$

$$\textcircled{3} \cos 2\theta \Rightarrow \cos 2\theta = 1 - 2\sin^2 \theta$$

$$\cos 2\theta = 1 - 2\left(-\frac{\sqrt{5}}{5}\right)^2$$

$$\cos 2\theta = 1 - 2\left(\frac{5}{25}\right)$$

$$\cos 2\theta = \frac{3}{5}$$

واجب 1 ص 28

① $\cos^4 x$

$$(\cos^2 x)^2 = \left[\frac{1}{2} (1 + \cos 2x) \right]^2 = \frac{1}{4} (1 + \cos 2x)^2$$

$$= \frac{1}{4} (1 + 2\cos 2x + \cos^2 2x)$$

$$= \frac{1}{4} \left(1 + 2\cos 2x + \frac{1}{2} (1 + \cos 4x) \right)$$

$$= \frac{1}{4} + \frac{1}{2} \cos 2x + \frac{1}{8} + \frac{1}{8} \cos 4x$$

$$= \frac{3}{8} + \frac{\cos 2x}{2} + \frac{\cos 4x}{8}$$

$$2) \sin^4 x \cos^2 x$$

$$[\sin^2 x]^2 \cdot \cos^2 x = \left[\frac{1}{2}(1 - \cos 2x) \right]^2 \cdot \frac{1}{2}(1 + \cos 2x)$$

$$\frac{1}{4}(1 - \cos 2x)^2 \cdot \frac{1}{2}(1 + \cos 2x) = \frac{1}{8} \cdot (1 - 2\cos 2x + \cos^2 2x)(1 + \cos 2x)$$

$$\frac{1}{8} \left[1 - 2\cos 2x + \cos^2 2x + \cos 2x - 2 \cdot \frac{1}{2}(1 + \cos 4x) + \cos^3 2x \right]$$

$$\frac{1}{8} \left[1 - 2\cos 2x + \overset{\uparrow}{\cos^2 2x} + \cos 2x - 1 - \cos 4x + \cos^3 2x \right]$$

$$\frac{1}{8} \left[-\cos 2x + \frac{1}{2} - \frac{1}{2}\cos 4x + \cos^3 2x \right]$$

$$\frac{1}{8} \left[-\cos 2x + \frac{1}{2} - \frac{1}{2}\cos 4x + \cos 2x \cdot \frac{1}{2}(1 + \cos 4x) \right]$$

$$\frac{1}{8} \left[-\cos 2x + \frac{1}{2} - \frac{1}{2}\cos 4x + \frac{1}{2}\cos 2x + \frac{\cos(2x) + \cos(6x)}{4} \right]$$

$$-\frac{1}{8}\cos 2x + \frac{1}{16} - \frac{1}{16}\cos 4x + \frac{1}{16}\cos 2x + \frac{1}{32}\cos 2x + \frac{1}{32}\cos 6x$$

$$-\frac{\cos 2x}{32} - \frac{\cos 4x}{16} + \frac{\cos 6x}{32} + \frac{1}{16}$$

$$\frac{2 + \cos 6x - 2\cos 4x - \cos 2x}{32}$$

p. 28 (اجب 1)

$$\sin^4 x \cos^2 x$$

$$= (\sin^2 x)^2 \cdot \cos^2 x$$

$$= \left(\frac{1 - \cos 2x}{2} \right)^2 \cdot \left(\frac{1 + \cos 2x}{2} \right)$$

نفرض $\cos 2x = c$

$$= \left(\frac{1 - c}{2} \right)^2 \cdot \left(\frac{1 + c}{2} \right)$$

$$= \frac{(1 - c)^2 (1 + c)}{8}$$

$$= \frac{(1 - 2c + c^2)(1 + c)}{8}$$

$$= \frac{1 - c - c^2 + c^3}{8}$$

$$c = \cos 2x$$

$$c^2 = \frac{1 + \cos 4x}{2}$$

$$c^3 = \cos^3(2x)$$

$$= 1 - c - \frac{1 + \cos 4x}{2} + \frac{3c + \cos 6x}{4}$$

$$= \frac{\cos 6x + 3\cos 2x}{4}$$

$$= \frac{\cos 6x + 3c}{4}$$

$$= \frac{4 - 4c - 2 - 2\cos 4x + 3c + \cos 6x}{8.4}$$

ضرب الكل بـ 4

$$= \frac{2 - c - 2\cos 4x + \cos 6x}{32}$$

$$\sin^4 x \cos^2 x = \frac{2 - \cos 2x - 2\cos 4x + \cos 6x}{32}$$

واجب 2 من 28 -8

$$1) \frac{\cos(\frac{\pi}{2} - x)}{\csc x} - \cos^2 x$$

$$= \frac{\sin x}{\csc x} - \cos^2 x$$

$$= \frac{\sin x}{\frac{1}{\sin x}} - \cos^2 x$$

$$= \sin^2 x - (1 - \sin^2 x)$$

$$= 2\sin^2 x - 1 = -\cos 2x$$

$$= -\cos 2x \quad \text{لأن } \cos 2x = 1 - 2\sin^2 x$$

$$2) \frac{\sec x - \cos x}{\sin x}$$

$$= \frac{\frac{1}{\cos x} - \cos x}{\sin x} = \frac{\frac{1 - \cos^2 x}{\cos x}}{\sin x}$$

$$= \frac{\sin^2 x}{\sin x \cos x} = \frac{\sin x}{\cos x}$$

$$= \tan x$$

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$$3) (\sin^2 x - \cos^2 x)(\sin^2 x + \cos^2 x)$$

$$= -(\cos 2x)(1)$$

$$= -\cos 2x$$

$$4) \frac{2\tan 7x}{1 - \tan^2 7x}$$

$$\tan(\theta + \theta) = \frac{\tan \theta + \tan \theta}{1 - (\tan \theta)(\tan \theta)}$$

$$= \frac{2\tan \theta}{1 - \tan^2 \theta} = \tan 14x$$

لأن $\tan 2\theta = \frac{2\tan \theta}{1 - \tan^2 \theta}$

واجب 24
-8

$$1) \sin \frac{\theta}{2} = + \sqrt{\frac{1 - \cos \theta}{2}} = \sqrt{\frac{1 - \frac{12}{13}}{2}} = \sqrt{\frac{\frac{1}{13}}{2}} = \frac{1}{\sqrt{26}}$$

$$\cos^2 \theta + \sin^2 \theta = 1$$

$$\cos^2 \theta + \frac{25}{169} = 1 \rightarrow \boxed{\cos \theta = \frac{12}{13}}$$



$$2) \cos \frac{\theta}{2} = + \sqrt{\frac{1 + \cos \theta}{2}} = \sqrt{\frac{1 + \frac{12}{13}}{2}} = \frac{5}{\sqrt{26}}$$

$$3) \sec 2\theta = \frac{1}{\cos 2\theta} = \frac{1}{2\cos^2 \theta - 1} = \frac{1}{2\left(\frac{144}{169}\right) - 1} = \frac{1}{\frac{119}{169}} = \frac{169}{119}$$

واجب 30

$$1) 1) 3 \cos 4x \cos 7x = \frac{3}{2} (\cos(-3x) + \cos(11x))$$

$$= \frac{3}{2} (\cos 3x + \cos 11x)$$

$$2) 8 \cos 3x \sin 6x = 8 \sin 6x \cos 3x = \frac{8}{2} (\sin(3x) + \sin(9x))$$

$$= 4 (\sin 3x + \sin 9x)$$

$$2) 1) \sin 3x + \sin 4x = 2 \sin\left(\frac{7}{2}x\right) \cos\left(\frac{-1}{2}x\right) = 2 \sin\frac{7}{2}x \cos\frac{x}{2}$$

$$2) \cos 3x + \cos 2x = 2 \cos\frac{5}{2}x \cos\frac{x}{2}$$

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$$\textcircled{1} \frac{\tan(20^\circ) + \tan(25^\circ)}{1 - \tan(20^\circ)\tan(25^\circ)} = \tan(20^\circ + 25^\circ)$$

$$= \tan(45^\circ) = \textcircled{1}$$

واجب صحت

$$\textcircled{2} \cos\left(\frac{5\pi}{12}\right)\cos\left(\frac{7\pi}{12}\right) - \sin\left(\frac{5\pi}{12}\right)\sin\left(\frac{7\pi}{12}\right)$$

$$= \cos\left(\frac{5\pi}{12} + \frac{7\pi}{12}\right) = \cos(\pi) = \textcircled{-1}$$

$$\textcircled{3} \sin\left(\frac{7\pi}{12}\right) = \sin\left(\frac{\pi}{4} + \frac{\pi}{3}\right)$$

$$= \sin\frac{\pi}{4}\cos\frac{\pi}{3} + \cos\frac{\pi}{4}\sin\frac{\pi}{3}$$

$$\frac{\sqrt{2}}{2} \cdot \frac{1}{2} + \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} = \textcircled{\frac{\sqrt{2} + \sqrt{6}}{4}}$$

$$\textcircled{4} \sin 75^\circ \sin 15^\circ$$

$$\frac{1}{2} [\cos(75^\circ - 15^\circ) - \cos(75^\circ + 15^\circ)]$$

$$\frac{1}{2} [\cos(60^\circ) - \cos(90^\circ)] = \frac{1}{2} \left[\frac{1}{2} - 0\right] = \textcircled{\frac{1}{4}}$$

$$\textcircled{5} \cos\left(\frac{23\pi}{12}\right) \Rightarrow \cos(2\pi - \pi) = \cos(\pi)$$

$$\cos\left(\frac{23\pi}{12}\right) = \cos\left(\frac{\pi}{12}\right) \Rightarrow \cos\left(\frac{\pi}{3} - \frac{\pi}{4}\right)$$

$$\cancel{\frac{1}{2}} \cos\frac{\pi}{3}\cos\frac{\pi}{4} + \sin\frac{\pi}{3}\sin\frac{\pi}{4} = \frac{1}{2} \cdot \frac{\sqrt{2}}{2} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{2}}{2} = \textcircled{\frac{\sqrt{6} + \sqrt{2}}{4}}$$

$$\textcircled{6} \tan 202.5^\circ = \tan(180^\circ + 22.5^\circ) \rightarrow \tan(180^\circ + x) = \tan x$$

$$\textcircled{\tan 202.5^\circ = \tan 22.5^\circ}$$

$$\textcircled{\theta = 45^\circ}$$

$$\tan 22.5^\circ = \frac{1 - \cos 45^\circ}{\sin 45^\circ} = \frac{1 - \frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = \frac{2 - \sqrt{2}}{\sqrt{2}} = \frac{4 - 2\sqrt{2}}{2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}}$$

$$\frac{4\sqrt{2} - 2 \cdot 2}{2 \cdot 2} = \frac{4\sqrt{2} - 4}{4} = \frac{4(\sqrt{2} - 1)}{4} = \textcircled{\sqrt{2} - 1}$$